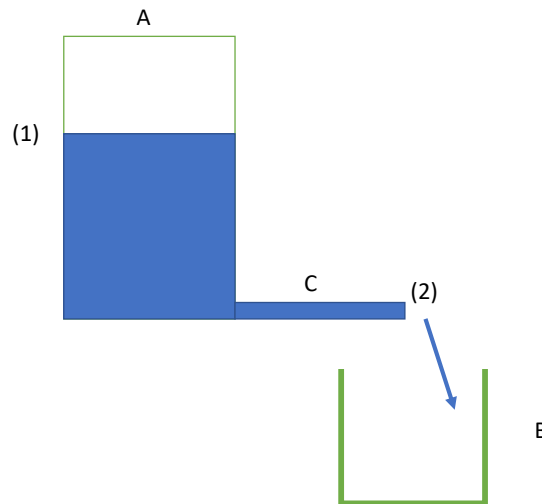


## Extra practice exam – Fluid Dynamics 2021

This practice exam consists of 4 questions. Questions marked with a [\*] can be considered slightly more difficult than regular exam questions.

### Question 1

A pressurized water reservoir A, whose free-surface is kept at a pressure  $2 \times 10^5$  Pa above the atmospheric pressure, discharges to another reservoir, B, open to the atmosphere, via a tube C, see drawing below.



The water free-surface level at the second reservoir is below the tube that comes from the pressurized reservoir A. The volume of reservoir B is  $1000 \text{ m}^3$ , exactly sufficient to empty the reservoir A. The cross-section area of reservoir A is  $50 \text{ m}^2$ . The cross-section area of the tube C is  $0.1 \text{ m}^2$ .

Calculate how long it takes to empty the reservoir A.

N.B. the level of water in A ( $h$ ) is a function of time, i.e.,  $h=h(t)$ .

Assume  $g = 10 \text{ m}\cdot\text{s}^{-2}$ ,  $\rho_{\text{water}}=1000 \text{ kg/m}^3$

### Question 2

A plate  $0,3 \text{ m}$  long and  $0,1 \text{ m}$  wide, with a thickness of  $12 \text{ mm}$  is made from stainless steel ( $\lambda=16 \text{ W}/(\text{m}\cdot\text{K})$ ). The top surface is exposed to an airstream temperature of  $20^\circ\text{C}$ . In an experiment the plate is heated by an electrical heater (also  $0,25 \text{ m}$  by  $0,1 \text{ m}$ ) positioned on the underside of the plate and the temperature of the bottom surface is kept by the heater at  $100^\circ\text{C}$ . The heater provides  $50 \text{ W}$ . The side surfaces are perfectly isolated.

Calculate the convective heat transfer coefficient  $h$ .

### Question 3\*

A PhD student of the department of organic chemistry recently developed a synthesis route for biodegradable surfactants on the basis of sugars. They asked a student in chemical engineering to estimate what the possibilities are for a (semi-) industrial process in a stirred tank reactor of  $1.25 \text{ m}^3$ . The student determined the rotational speed and the dissipated power of the stirrer at optimal production circumstances in a geometrical similar (= equally shaped) tank reactor of 10 liters. The motor power  $P_o$  (W) is a function of the rotational speed of the stirrer  $N$  ( $\text{s}^{-1}$ ), the density of the medium  $\rho$  ( $\text{kg/m}^3$ ), the viscosity of the medium  $\eta$  ( $\text{Pa s}$ ) and the diameter of the reactor  $D$  (m). The experiments show that optimal conditions can be reached in the 10 liter reactor at a stirrer speed of 150 RPM and at a motor power of 70 Watt.

- How many dimensionless numbers do you expect you need to describe the power of the stirrer and why?
- Give a dimensionless expression for  $P_o$ .
- What do you recommend for the stirrer speed in the production reactor?
- What motor power is needed in the production reactor?

### Question 4\*

Two litres of water ( $\rho = 1 \text{ Kg}\cdot\text{L}^{-1}$ ) per second flow through a horizontal pipe with a constant diameter  $D = 5 \text{ cm}$ . There is an obstacle in the pipe which forms an (extra) element of resistance to the flow; conversely, the flow exercises a force  $F$  on the obstacle. With the help of a U-form pressure sensor, similar to the ones used by the Venturi tubes, the pressure difference between two points (1 and 2) before and after the obstacle can be measured. Mercury ( $\rho_{\text{Hg}} = 13,5 \text{ Kg}\cdot\text{L}^{-1}$ ) is used in the U-form pressure sensor. The mercury level difference in the two sides of the pressure sensor is 8 mm.

Calculate the force  $F$  that the flowing water is exercising on the obstacle.  
Assume  $g = 10 \text{ m}\cdot\text{s}^{-2}$ .

Hint: write a momentum balance between points 1 and 2.

